

Oxygen Permeability and Structural Stability of a Novel Tantalum-Doped Perovskite $\text{BaCo}_{0.7}\text{Fe}_{0.2}\text{Ta}_{0.1}\text{O}_{3-\delta}$

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Dense $\text{BaCo}_{0.7}\text{Fe}_{0.2}\text{Ta}_{0.1}\text{O}_{3-\delta}$ (BCFT) perovskite membranes were successfully synthesized by a simple solid state reaction. In situ high-temperature X-ray diffraction indicated the good structure stability and phase reversibility of BCFT at high temperatures. The thermal expansion coefficient (TEC) of BCFT was determined to amount $1.02 \times 10^{-5} \text{ K}^{-1}$, which is smaller than those of $\text{Ba}_{0.5}\text{Sr}_{0.5}\text{Co}_{0.8}\text{Fe}_{0.2}\text{O}_{3-\delta}$ (BSCF) ($1.15 \times 10^{-5} \text{ K}^{-1}$), $\text{SrCo}_{0.8}\text{Fe}_{0.2}\text{O}_{3-\delta}$ (SCF) ($1.79 \times 10^{-5} \text{ K}^{-1}$), and $\text{BaCo}_{0.4}\text{Fe}_{0.4}\text{Zr}_{0.2}\text{O}_{3-\delta}$ (BCFZ) ($1.03 \times 10^{-5} \text{ K}^{-1}$). It can be seen that the introduction of Ta ions into the perovskite framework could effectively lower the TEC. Thickness dependence studies of oxygen permeation through the BCFT membrane indicated that the oxygen permeation process was controlled by bulk diffusion. A membrane reactor made from BCFT was successfully operated for the partial oxidation of methane to syngas at 900°C for 400 h without failure and with the relatively high, stable oxygen permeation flux of about 16.8 ml/min cm^2 . © 2009 American Institute of Chemical Engineers AICHE J, 56: 604–610, 2010

Keywords: perovskite, oxygen separation, mixed conductor, membrane, POM

Introduction

In recent years, mixed-conducting ceramic oxides with oxygen ionic and electronic conductivity have attracted increasing attention due to the potential applications in oxygen separation from air,^{1–9} in the partial oxidation of methane (POM) to syngas,^{10–16} in the selective oxidation of hydrocarbons,^{17–19} for the power plants with carbon dioxide sequestration.^{20,21} Especially, the promising application in the POM to synthesis gas (a $\text{H}_2\text{:CO}$ mixture 2:1) seems to be an attractive route for upgrading natural gas. Promising membranes should not only possess high-oxygen permeabil-

ity but also good structural stability to withstand the harsh working conditions, such as the reducing atmosphere of synthesis gas or steam. During the last 10 years, much progress was achieved to meet the aforementioned requirements. $\text{SrCo}_{0.8}\text{Fe}_{0.2}\text{O}_{3-\delta}$ (SCF) possesses high-oxygen permeability, and the oxygen permeation fluxes can reach 3.1 ml/min cm^2 under an air/He oxygen gradient at 850°C with 1.0 mm membrane thickness.²² Unfortunately, SCF shows low-structural stability in a reducing atmosphere. To improve the structural stability, many researchers doped SCF with higher valence metal ions such as: $\text{A} = \text{Ba}^{2+}$, La^{2+} , Ca^{2+} , $\text{B} = \text{Ti}^{4+}$, Zr^{4+} , Nb^{5+} . Yang's group^{23–27} developed a series of materials based on $\text{BaTi}_{0.2}\text{Co}_{0.5}\text{Fe}_{0.3}\text{O}_{3-\delta}$ (BTCF) and $\text{BaCo}_{0.4}\text{Fe}_{0.4}\text{Zr}_{0.2}\text{O}_{3-\delta}$ (BCFZ). By partially substituting Ba by Sr, a novel material named $\text{Ba}_{0.5}\text{Sr}_{0.5}\text{Co}_{0.8}\text{Fe}_{0.2}\text{O}_{3-\delta}$ (BSCF), which shows high-oxygen permeability and good

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operation stability in the POM reaction, was developed.^{23,24} ZrO₂ or YSZ-doped SCF had been proven to have a high-oxygen permeation flux, stable lattice structure, and high-mechanical strength,²⁸ although a potential problem of the thermal mismatch between two phases in SCF were not solved yet. To further improve the stability of the membrane materials, cations with constant valence (Zr⁴⁺, Ga³⁺, and Al³⁺) were used to partially substitute the reducible B-site ions (Co⁴⁺/Co³⁺ and Fe⁴⁺/Fe³⁺).^{29–32} However, some researchers found that the pure-phase perovskite was hard to obtain as the large ions (such as Zr) were not easy to bring into the perovskite structure due to the large ionic radius.^{9,26,32} To prepare a pure-phase perovskite structure, some ions with small size were used. For example, Wang et al.³³ found that Zn can be easily brought into the perovskite structure and developed a Ba_{0.5}Sr_{0.5}Fe_{0.8}Zn_{0.2}O_{3–δ} membrane, which shows a high-oxygen permeation flux and an excellent phase stability under low-oxygen partial pressure. Recently, a novel perovskite-type mixed-conducting membrane based on SrSc_{0.05}Co_{0.95}O_{3–δ} with good oxygen permeability was reported.^{34,35} However, Sc is a very expensive metal, which might limit the application of this material.

Nagai et al.³⁶ found that Nb is the best candidate for the cation substitution of SrCo_{1–x}M_xO_{3–δ}. Shao et al.³⁷ found that the substitution of Ba for Sr on the A-site can prevent the long range ordering of oxygen vacancies, thus improving the stability of the perovskite. Subsequently, a novel perovskite of the composition BaCo_{0.7}Fe_{0.2}Nb_{0.1}O_{3–δ} was developed, and it was found that BaCo_{0.7}Fe_{0.2}Nb_{0.1}O_{3–δ} exhibits a high-oxygen permeability and good phase stability.^{38,39} In this article, Ta was chosen for the substitution on the B-site, because Ta is the same group element as Nb and, furthermore, the thermal expansion coefficient (TEC) of Ta₂O₅ ($6.6 \times 10^{-6} \text{ K}^{-1}$) is lower than that of Nb₂O₅ ($7.07 \times 10^{-6} \text{ K}^{-1}$). Therefore, we can expect that the incorporation of the pentavalent Ta⁵⁺ ion in the perovskite structure can lower the TEC and improve the stability. The perovskite BaCo_{0.7}Fe_{0.2}Ta_{0.1}O_{3–δ} (BCFT) was synthesized by a solid state reaction. The phase structure and the oxygen permeability under air/He gradient and POM reaction were investigated. The rate-limiting step for the oxygen transport was clarified and the operation stability was studied.

Experimental

The BCFT powder samples were synthesized using a solid state reaction. BaCO₃, Co₂O₃, Fe₂O₃, and Ta₂O₅ (all reagents with A.R. purity) were weighted according to their stoichiometry and mixed in an agate mortar for 1.5 h and then ball-milled for 24 h in ethanol. Then, the mixtures were calcined at 950°C for 10 h with heating and cooling rates of 2°C/min. Then, the primary powders were mixed finely in an agate mortar and sintered at 950°C for 10 h again, with the same heating and cooling rates as in the first calcination.

The as-synthesized powders were pressed to disk membranes under a pressure of 18–24 MPa in a stainless steel module with a diameter of 16 mm. The green disks were sintered at 1000°C for 10 h. The densities of the sintered membranes were determined by the Archimedes method using ethanol. Only those membranes that had relative den-

sities higher than 95% were chosen for the oxygen permeation studies.

The crystal structures and lattice constant of the BCFT perovskite were characterized by *in situ* high-temperature X-ray diffraction (XRD) (PHILIPS-PW1710) using Cu K α radiation. The sample was tested in a high-temperature cell (Bühler HDK 2.4 with REP 2000) with a heated Pt sample holder upto 1000°C in different atmospheres (air, 2% O₂ in Ar, and pure Ar). The Pt heater was used as the sample holder and a thermal coupler was connected directly on the Pt heater (i.e., sample holder). The heating and cooling rates amounted to 5°C/min. At each temperature step, the temperature was held for 70 min. Data were collected in a continuous scan mode in the range of 20°–80° with intervals of 0.05°. The peaks of Pt were used as an internal standard to calculate the lattice constant of the BCFT perovskite. The element analysis of fresh and spent membranes was performed by energy dispersive X-ray spectroscopy (SEM-EDXS, Jeol-JSM-6700F).

Oxygen temperature-programmed desorption (O₂-TPD) was performed on a Micromeritics AutoChem 2920TM. Before O₂ desorption, the samples (about 1.0 g, particle size = 40–60 mesh) were pretreated in flowing O₂ (99.999%, 30 ml/min) at 950°C for 2 h. Then, the temperature was cooled down to 40°C at a rate of 10°C/min, and O₂-TPD was performed from 50°C to 1000°C with a heating rate of 10°C/min, where He (99.999%, 30 ml/min) was used as the carrier gas. The amount of desorbed oxygen was detected by gas chromatography using a thermal conductivity detector. To investigate the reversibility of oxygen adsorption and desorption, after O₂-TPD, the samples were pretreated again under flowing O₂ at 950°C, and then the next O₂-TPD run was performed again. After the last run, the samples were characterized by XRD.

The oxygen permeation was conducted on a self-made high-temperature oxygen permeation cell, as shown in Figure 1. The membrane was sealed on a quartz tube ($\varnothing = 16 \text{ mm}$). Another quartz tube ($\varnothing = 24 \text{ mm}$) served as the air side of the permeator. A tubular furnace was used to heat the permeator. The temperature was controlled by a microprocessor temperature controller (Model AI-708, Xiamen Yudian Electronics Technology Research Institute, China) within $\pm 1^\circ\text{C}$ of the set points and monitored by a K-type thermocouple positioned near the discs. A gold paste from the Institute of Platinum Manufactory (Guizhou, China) was used as the binding agent to seal the disk onto a quartz tube at 950°C for 5 h. The inlet gas flow rates were controlled by mass flow controllers (model D07-7A/ZM, Beijing Jianzhong Machine Factory, China). Synthetic air was fed to the air side of the permeator and high-purity He (>99.995%) was fed to the sweep side of the permeator. A gas chromatograph (Shimadzu GC-14B) equipped with a TDX-01 column for the separation of oxygen and nitrogen was connected to the exit of the sweep side. The GC was frequently calibrated using standard gases like oxygen and helium to ensure reliability of the experimental data. The leakage of oxygen was subtracted when the oxygen permeation flux was calculated. Assuming that leakage of nitrogen and oxygen through pores or cracks is in accordance with Knudsen diffusion, the fluxes of leaked N₂ and O₂ are related by Eq. 1 as follows:

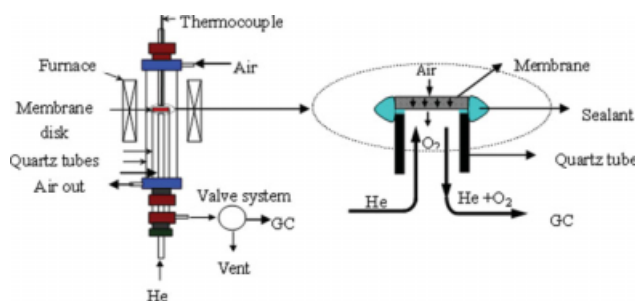


Figure 1. Permeation cell used for the oxygen permeation at high temperatures.

[Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

$$J_{N_2}^{\text{Leak}} : J_{O_2}^{\text{Leak}} = \sqrt{\frac{32}{28}} \times \frac{0.79}{0.21} = 4.02 \quad (1)$$

The oxygen permeation flux was then calculated as follows:

$$J_{O_2} (\text{ml/min} \cdot \text{cm}^2) = \left(C_{O_2} - \frac{C_{N_2}}{4.02} \right) \times \frac{f}{S} \quad (2)$$

where C_{O_2} , C_{N_2} are the oxygen and nitrogen concentrations calculated from GC calibration, f is the total flow rate of the outlet on the sweep side, which was measured by a soap film meter. S is the membrane area.

Results and Discussion

In situ XRD provides an effective and direct way to characterize the high-temperature structure changes during increasing and decreasing temperatures. Figure 2 shows the XRD patterns of BCFT in air for increasing temperature from 30°C to 1000°C indicating that BCFT remains in the perovskite structure over the examined temperature range. The XRD patterns during the temperature increase and decrease are identical. In turn, this means that BCFT exhibits good phase reversibility and structure stability in air at high temperatures, which can also be proven by the multirun O_2 -TPD.

During the oxygen permeation experiments, one side of the membrane was exposed to synthetic air (high-oxygen partial pressure); the other side of the membrane was exposed to the sweep gases Ar or He (low-oxygen partial pressure). The proven phase stability of BCFT in air alone is not enough to recommend BCFT as a candidate for oxygen separation. Therefore, it is necessary to study the high-temperature phase stability of BCFT at low-oxygen partial pressure, e.g., 2% O_2 in Ar or pure Ar, as shown in Figure 3. The XRD patterns of BCFT powder at 900°C under different oxygen partial pressures show that BCFT can remain in its perovskite structure both in air and 2% O_2 in Ar, and even in pure Ar with an oxygen partial pressure $\leq 1 \times 10^{-5}$ bar. These results indicate that BCFT possesses an excellent phase stability at high temperatures not only in air but also in atmospheres with an oxygen partial pressure $\leq 1 \times 10^{-5}$ bar. In fact, the oxygen concentration at the sweep side during the oxygen permeation is around 1–3% above 800°C.

Therefore, it is expected that a BCFT membrane can be steadily operated in the oxygen separation for a long time.

Figure 4 shows the lattice constants of BCFT at various temperatures determined from the XRD data in air. From Figure 4, it can be seen that the lattice constant increases linearly with temperatures for both increasing and decreasing temperatures. Within the temperature range studied, the change of the lattice constant of BCFT is 0.99%. The thermal expansion coefficient (TEC) was calculated following the definition $\frac{d(\Delta a/a_0)}{dT}$ (a , lattice constant; a_0 , lattice constant at room temperature). From Figure 4, the average TEC of BCFT is found to be $1.02 \times 10^{-5} \text{ K}^{-1}$. In our previous study,⁴⁰ by the same *in situ* high-temperature XRD, it was found that the TECs of BSCF, SCF, and BCFZ are $1.15 \times 10^{-5} \text{ K}^{-1}$, $1.79 \times 10^{-5} \text{ K}^{-1}$, and $1.03 \times 10^{-5} \text{ K}^{-1}$, respectively. It can be seen that the TEC of BCFT is smaller than SCF and BCFS, and even slightly smaller than that of BCFZ. The lower TEC is beneficial for the operation stability of BCFT membrane.

The O_2 -TPD technique provides not only an effective way to characterize the oxygen absorption/adsorption properties of the ceramic oxides but also an indirect evidence for the structure stability. Figure 5 presents the multirun O_2 -TPD

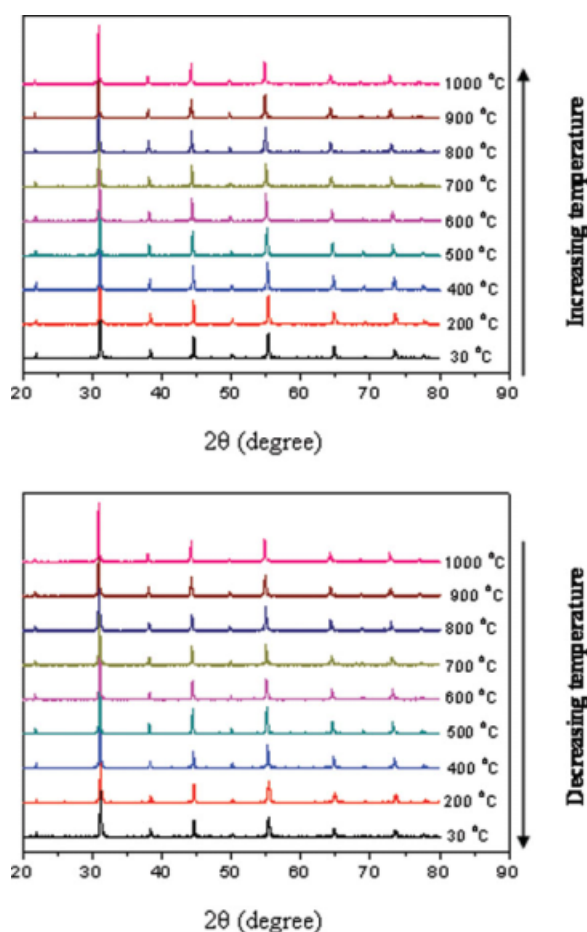


Figure 2. *In situ* XRD patterns of BCFT under air during increasing and decreasing temperatures.

Heating and cooling rate = 5°C/min, equilibration time at each temperature: 70 min for recording the XRD. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

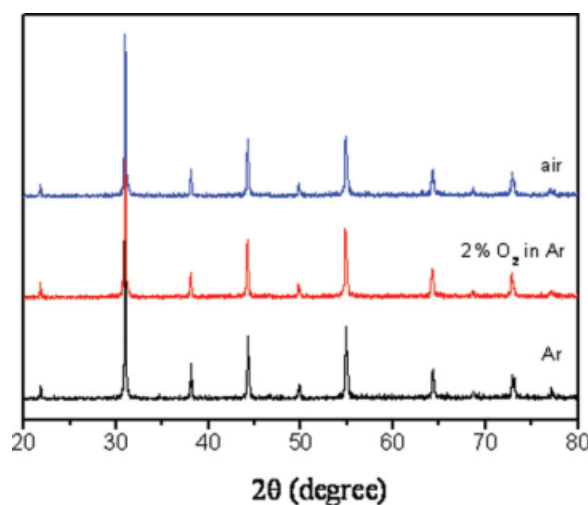


Figure 3. *In situ* XRD patterns of the BCFT under different atmospheres at 900°C.

Equilibration time: 70 min before recording XRD at each temperature. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

profiles of BCFT. As shown in Figure 5, two O_2 desorption peaks can be seen in the BCFT sample, one peak is between 250 and 500°C and the other between 830 and 1000°C. The low-temperature peak is attributed to the reduction of the high-valence states Fe^{4+} and/or Co^{4+} to Fe^{3+} and/or Co^{3+} . The high-temperature peak is attributed to the reduction of Fe^{3+} and/or Co^{3+} to Fe^{2+} and/or Co^{2+} . The reversibility of oxygen adsorption and desorption is a significant factor for a stable structure. The multirun O_2 -TPD profiles in Figure 5 have the same profiles as the first-run one. It means that BCFT possesses good reversibility for the oxygen adsorption and desorption. After the multirun O_2 -TPD, the sample is characterized by XRD, as shown in Figure 6. It can be seen that the perovskite structure was kept, which indicates that the BCFT exhibits an excellent structure stability and phase reversibility. The result is in agreement with the finding of *in situ* high-temperature XRD.

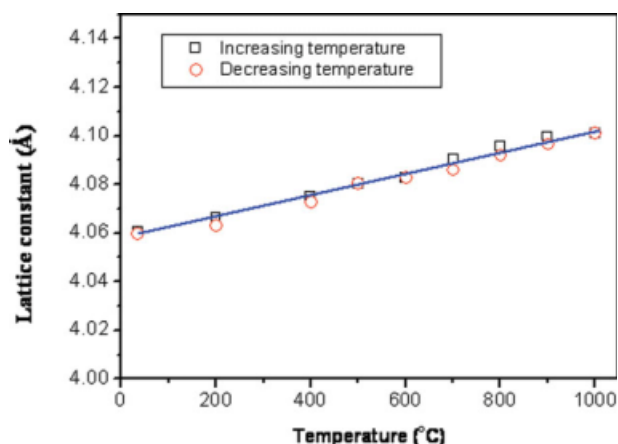


Figure 4. Temperature dependence of the lattice constants for BCFT.

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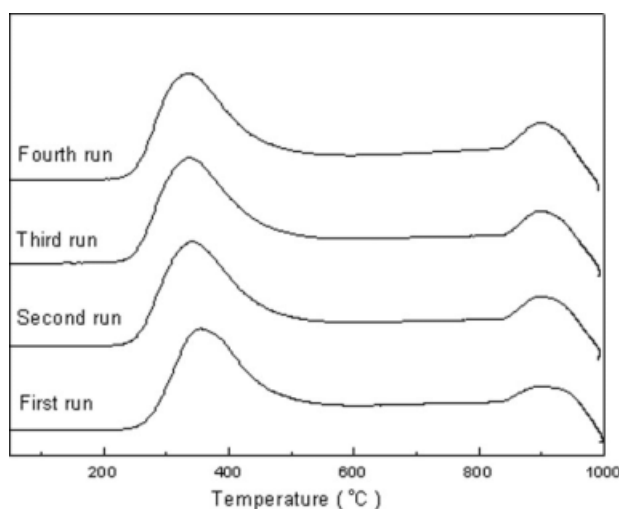


Figure 5. Multirun O_2 -TPD profiles of the BCFT.

Good oxygen permeability is an important factor for the application of dense perovskite membranes and, therefore, the oxygen permeability of the BCFT membranes was investigated in detail. The oxygen permeation fluxes through the dense BCFT membranes of different thicknesses at different temperatures are presented in Figure 7. It can be seen that the oxygen permeation fluxes increase distinctly with increasing temperature. Furthermore, it can also be seen that the oxygen permeation fluxes increase remarkably with decreasing membrane thickness. The oxygen permeation flux through the membrane with a thickness of 1.2 mm was 1.05 ml/cm^2 min at the oxygen partial pressure of 0.021 bar on the sweep side, the J_{O_2} through the membrane with a thickness of 0.60 mm can reach 2.22 ml/cm^2 min at the oxygen partial pressure of 0.043 bar on the sweep side. It is interesting to note that the J_{O_2} through a membrane with a thickness of 1.0 mm was 1.58 ml/min cm^2 at 950°C, which is 1.8

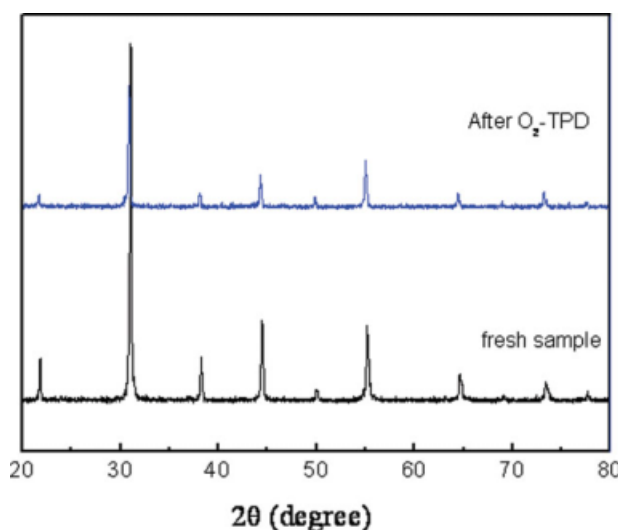


Figure 6. XRD patterns for the fresh BCFT and the sample after multirun O_2 -TPD.

[Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

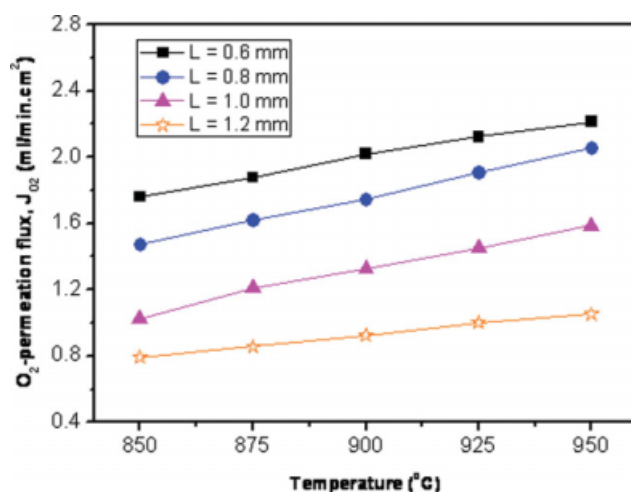


Figure 7. Temperature dependence of the oxygen permeation fluxes through BCFT membranes of different thicknesses.

[Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

times more than that through a BCFZ membrane (0.9 ml/min cm^2) at 950°C under a similar oxygen gradient as driving force (150 ml/min synthetic air, 30 ml/min He, thickness = 1.0 mm).³²

If the bulk diffusion is the limiting step for the oxygen permeation, the oxygen permeation flux J_{O_2} through the mixed electronic–ionic conducting membrane can be theoretically expressed by the following equation:

$$J_{\text{O}_2} = \frac{2.303RT\sigma_e\sigma_i}{16F^2(\sigma_e + \sigma_i)L} \log \frac{P_h}{P_l} \quad (3)$$

where R , F , T , and L denote the gas constant; Faraday constant; temperature; and thickness of the membrane, respectively. P_h and P_l are the oxygen partial pressures on the air and sweep sides. Note that the oxygen partial pressure on the sweep gas side depends on the oxygen permeation flux and the He flow rate. σ_e and σ_i are the electronic and ionic conductivity, respectively. Therefore, a plot of $J_{\text{O}_2}/\log(P_h/P_l)$ against the reciprocal of the membrane thickness ($1/L$) is linear and goes through the origin of the coordinates if the limiting step of the oxygen permeation is bulk diffusion. To determine the rate-limiting step of the oxygen permeation of BCFT, the oxygen permeation fluxes through membranes of different thickness were measured as a function of temperature. From Figure 8, it follows that the oxygen permeation fluxes increase linearly with $1/L$, which reveals that the overall oxygen permeation is limited by the bulk diffusion of the oxygen ions. The results demonstrate that a high-oxygen permeation flux for the commercial applications can be obtained by decreasing the membrane thickness such as via spinning the membrane in a hollow fiber configuration with an asymmetric structure.^{1–6}

Figure 9 shows the oxygen permeation flux through the BCFT membrane as a function of time at 900°C . It was found that the oxygen permeation fluxes were steady during 120 h of operation. After the 120 hours' operation, both sides of the

membrane were characterized by XRD. Figure 10 shows the XRD patterns of the membrane surface exposed to the air side and the He side. It was found that the membrane surface exposed to the He side kept the cubic perovskite structure, whereas on the membrane surface exposed to the air side some impurity peaks besides the cubic perovskite structure were found. We polished the membrane surface exposed to the air side several micrometers in depth, then XRD was used to characterize the structure. Only the cubic perovskite structure was observed, as shown in Figure 10. This finding indicates that the impurities were only on the membrane surface. EDXS analysis found around 3.82 atom% sulfur on the membrane surface exposed to the air side, most probably as BaSO_4 . The sulfur stems were possibly from the traces of sulfur in the fed air. It should be pointed out that similar concentrations of sulfur on the perovskite membrane surface usually lead to a blockade of the oxygen permeability.⁴¹ However, for BCFT membrane, it seems that the presence of sulfur has no significant poisoning influence on the oxygen permeability.

To demonstrate the stability of BCFT under a reducing atmosphere, a BCFT membrane was used to construct a reactor for the POM to syngas. The long-term POM reaction in a BCFT membrane reactor was performed at 900°C with 48% methane diluted by helium at the flow rate of 50 ml/min. A methane conversion of 99%, CO selectivity of 94%, and an oxygen permeation flux of around $16\text{--}17 \text{ ml/min cm}^2$ were achieved. The long-term time dependence of the oxygen permeation flux is shown in Figure 11. During the 400 h run, the oxygen permeation was fairly stable with a value of about 16.8 ml/min cm^2 , demonstrating the excellent performance of the membrane reactor. The excellent phase reversibility of the BCFT oxide might stabilize the membrane reactor under the highly reducing atmosphere, such as under synthesis gas conditions.

Conclusions

In this study, BCFT powders are synthesized in a solid state reaction. The results of *in situ* high-temperature XRD

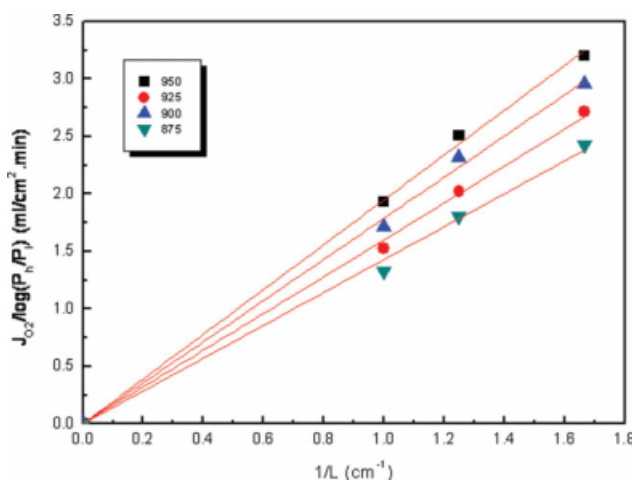


Figure 8. Relationship between oxygen permeation fluxes and the reciprocal thickness of BCFT membranes at different temperatures.

[Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

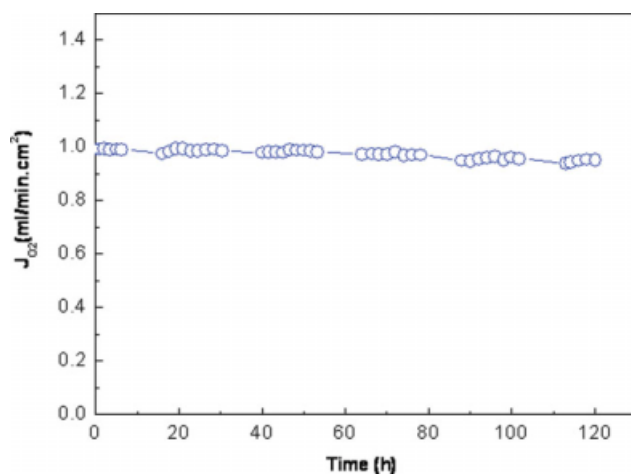


Figure 9. Oxygen permeation flux through BCFT as a function of time at 900°C.

Membrane thickness = 1.0 mm, air flow rate = 150 ml/min, He flow rate = 30 ml/min. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

and multirun O_2 -TPD indicate that the BCFT membrane has good structure stability and phase reversibility in air at high temperatures. The thermal expansion coefficient (TEC) of $BaCo_{0.7}Fe_{0.2}Ta_{0.1}O_{3-\delta}$ of $1.02 \times 10^{-5} K^{-1}$ is calculated from the *in situ* high-temperature XRD. It is found to be smaller than those of $Ba_{0.5}Sr_{0.5}Co_{0.8}Fe_{0.2}O_{3-\delta}$ ($1.15 \times 10^{-5} K^{-1}$), $SrCo_{0.8}Fe_{0.2}O_{3-\delta}$ ($1.79 \times 10^{-5} K^{-1}$), and $BaCo_{0.4}Fe_{0.4}Zr_{0.2}O_{3-\delta}$ ($1.03 \times 10^{-5} K^{-1}$), which indicates that BCFT shows a good operation stability. Oxygen permeation fluxes are measured in the range of 850–950°C. Thickness dependence of oxygen permeation of the membrane indicates that oxygen permeation is controlled by bulk diffusion in the range of thicknesses of 0.6–1.2 mm. After 120 h oxygen permeation, it is found that the membrane surface exposed to the He side remains completely in the cubic

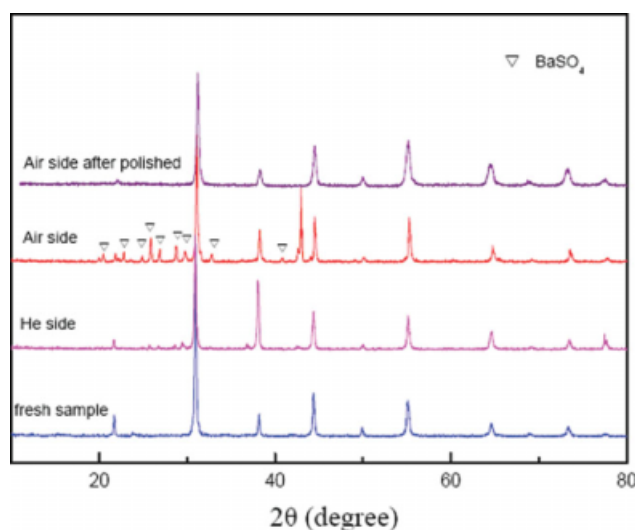


Figure 10. XRD patterns of the fresh and spent BCFT membranes.

[Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

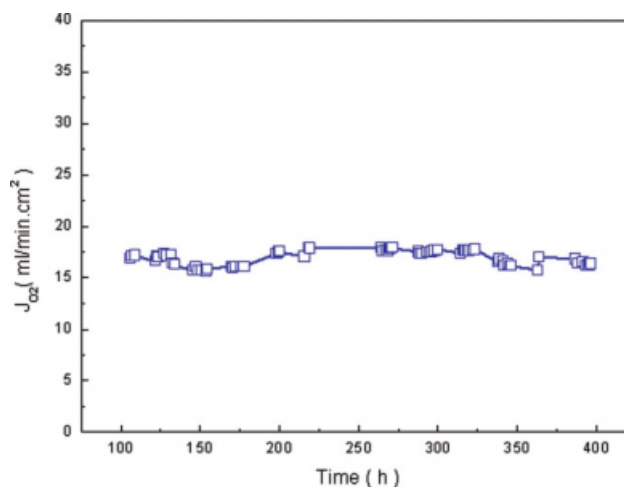


Figure 11. Long-term time dependence of oxygen permeation flux through BCFT membrane at 900°C under POM reaction conditions.

Sweep side: 48% methane diluted by He at a constant flow rate of 50 ml/min; air side: Air flow rate = 200 ml/min. 0.3 g Ni-based catalyst. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com.]

structure while around 3.82 atom% sulfur are detected by EDXS on the membrane surface exposed to the synthetic air side, most probably as $BaSO_4$. Fortunately, the presence of sulfur has no significant effect on the oxygen permeability. A BCFT membrane reactor was successfully operated at 900°C for around 400 h in the POM reaction with fairly stable oxygen permeation flux of about 16.8 ml/min cm^2 . The excellent phase reversibility of the material stabilized the membrane reactor under syngas atmosphere.

Acknowledgments

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Notation

- $J_{N_2}^{\text{Leak}}$ = leaked nitrogen flux (ml/min cm^2)
- $J_{O_2}^{\text{Leak}}$ = leaked oxygen flux (ml/min cm^2)
- J_{O_2} = oxygen permeation flux (ml/min cm^2)
- C_{O_2} = oxygen concentration (%)
- C_{N_2} = nitrogen concentration (%)
- \dot{f} = total flow rate of the outlet on the sweep side (ml/min)
- S = membrane area (cm^2)
- a = lattice constant (\AA)
- a_0 = lattice constant at room temperature (\AA)
- P_h = oxygen partial pressures on the air side (bar)
- P_l = oxygen partial pressure the sweep side (bar)
- P_o = standard pressure ($P_o = 1 \text{ bar}$)
- R = gas constant ($R = 8.3145 \text{ J/mol K}$)
- F = Faraday constant (C/mol)
- T = temperature ($^\circ\text{C}$)
- L = thickness of the membrane (mm)

Greek letters

- δ = oxygen nonstoichiometry, $0 < \delta < 1$
- σ_i = ion conductivity (S/m)
- σ_e = electronic conductivity (S/m)

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